

17) a)  $\mu = 80$      $\sigma = 10$

1)  $H_0: \mu_{\text{score after training}} = 80$

(No effect of training on problem solving ability)

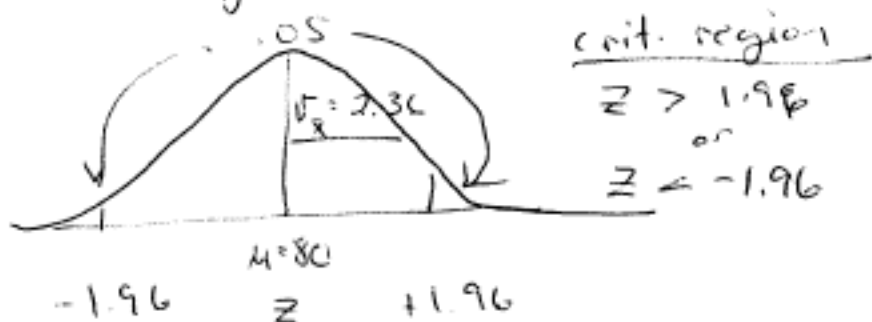
$H_1: \mu_{\text{score after training}} \neq 80$

(There is an effect of training on problem solving)

$\alpha = .05$

2) Set criteria

$$\begin{aligned} \sigma_{\bar{x}} &= \frac{\sigma}{\sqrt{n}} = \frac{10}{\sqrt{8}} \\ &= \frac{10}{2.83} \\ &= 3.54 \end{aligned}$$



3) Collected sample data & compute statistic

$$\begin{aligned} z_{\text{obt}} &= \frac{\bar{x} - \mu}{\sigma_{\bar{x}}} = \frac{84.44 - 80}{2.36} \\ &= \frac{4.44}{2.36} = 1.88 \end{aligned}$$

4) Fail to reject  $H_0$  because  $z_{\text{obt}}$  of 1.88 is not in the critical region

5) Conclusion: There was no significant effect of the training on problem solving,  $z = 1.88$ ,  $p > .05$ .

17 b) with one-tailed test

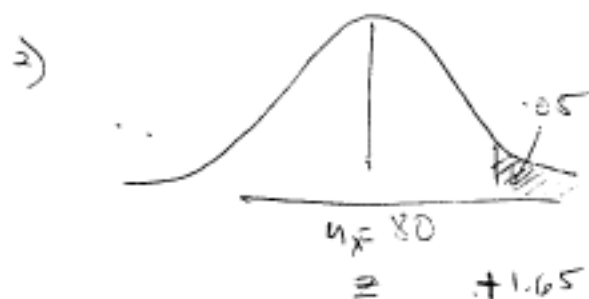
1)  $H_0: \mu_{\text{after train}} \leq 80$

(training does not improve prob. sol.)

$H_1: \mu_{\text{after train}} > 80$

(training ~~does~~ improves prob. solving)

$\alpha = .05$



critical region  
 $z > +1.65$

$\therefore$  we would reject  $H_0$  because  $z_{\text{obt}}$  of 1.88 is in the critical region

for  $\alpha = .025$

$z_{\text{crit}} = +1.96$

$\therefore$  again we would not reject  $H_0$

Prob. 18)  $\mu = 26$  anagrams solved  $\sigma = 4$

1)  $H_0: \mu_{\text{anxiety-ridden perform.}} \geq 26$

(anxiety does not decrease # anagrams solved)

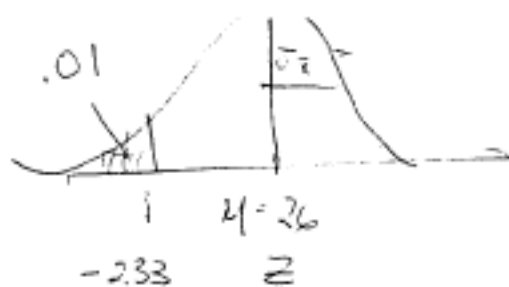
$H_1: \mu_{\text{anxiety-ridden performance}} < 26$

(anxiety decreases the # of anagrams solved)

$\alpha = .01$  one-tailed

18) 2) crit region

$$z < -2.33$$



$$\begin{aligned} \sigma_{\bar{x}} &= \frac{1.017}{\sqrt{14}} \\ &= \frac{1.017}{3.74} \\ &= \underline{\underline{1.017}} \end{aligned}$$

3) sample data  $\bar{x} = 23.36$  anagrams  $n = 14$

$$z_{\text{obt.}} = \frac{\bar{x} - \mu}{\sigma_{\bar{x}}} = \frac{23.36 - 26}{1.017} = \underline{\underline{-2.47}}$$

4) reject  $H_0$  (because  $z_{\text{obt}}$  of  $-2.47$  is in the critical region)

5) conclusion: Anxiety significantly reduces # of anagrams solved,  $z = -2.47$ ,  $p < .01$ , one-tailed test

b) two-tailed test

1)  $H_0: \mu = 26$   
anagram-solved

(No effect of training on # anag. solved)

$H_1: \mu_{\text{anagram-solved}} \neq 26$

(Effect of train. on # anag. probs solved)

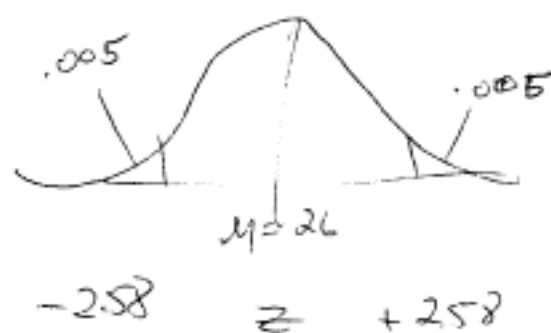
$$\alpha = .01$$

2) crit region

$$z > +2.58$$

or

$$z < -2.58$$



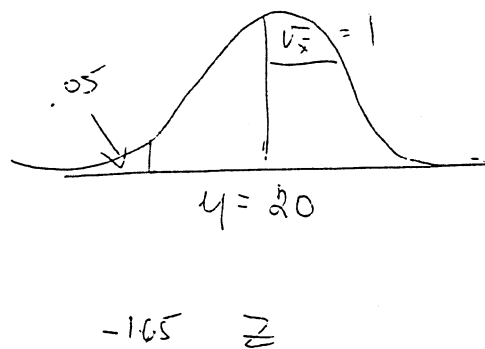
Fail to reject  $H_0$  (or retain)

25) Motor Skills task  $\mu = 20$ ,  $\sigma = 4$

- 1)  $H_0: \mu_{\text{perf. score with self awareness}} \geq 20$  (self-awareness does not decrease performance)  
 $H_1: \mu_{\text{perf score w self awareness}} < 20$  (self awareness decreases performance)  
 $\alpha = .05$ , one-tailed test

2) Crit. region

$$Z < -1.65$$



sampling dis

$$\begin{aligned} \sigma_{\bar{x}} &= \frac{\sigma}{\sqrt{n}} \\ &= \frac{4}{\sqrt{16}} \\ &= \frac{4}{4} = 1 \end{aligned}$$

3) Sample data

$$x = 15.5 \quad z_{\text{obt.}} = \frac{\bar{x} - \mu}{\sigma_{\bar{x}}} = \frac{15.5 - 20}{1} = -4.5$$

4) Decision: Reject  $H_0$  because  $z_{\text{obt.}}$  of  $-4.5$  in C.R.

5) Conclusion: Self-awareness significantly reduced performance on the motor skills task,  $z = -4.5$ ,  $p < .05$ , one-tailed test.

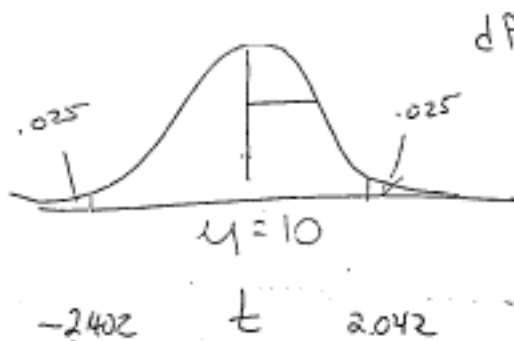
- ③
- As variability increases,  $t$  becomes smaller (closer to zero)
  - As sample size increases, the standard error decreases and the  $t$  value increases
  - The larger the diff bet  $\bar{x}$  and  $\mu$ , the larger the  $t$  value.

①①  $M = 10$  sample  $n = 36$

- $H_0: \mu_{\text{test}} = 10$  (no different from chance)  
 $H_1: \mu_{\text{test}} \neq 10$  (different from chance)

$\alpha = .05$

- Crit region  
 $t > 2.402$   
or  
 $t < -2.402$



$df = 35$

$\bar{x} = 13.5$   
 $s^2 = 144$   
 $s = 12$

- $t_{(35)} = \frac{\bar{x} - \mu}{\frac{s}{\sqrt{n}}} = \frac{13.5 - 10}{2} = \frac{3.5}{2} = 1.75$

$s_2 = \frac{s}{\sqrt{n}}$   
 $= \frac{12}{\sqrt{36}} = \frac{12}{6} = 2$

- Retain  $H_0$  because  $t_{\text{obt}}$  of 1.75 is not in crit region.

- Conclusion: Students' scores are not significantly different than what we would expect by chance,  $t(35) = 1.75$ ,  $p > .05$

12)  $\mu = 7.9$

current sample  $\bar{x} = 7.3$   $SS = 99$   
 $n = 100$

Step 1  $H_0: \mu_{\text{score now}} = 7.9$

(no change from 10 years ago)

$H_1: \mu_{\text{score now}} \neq 7.9$

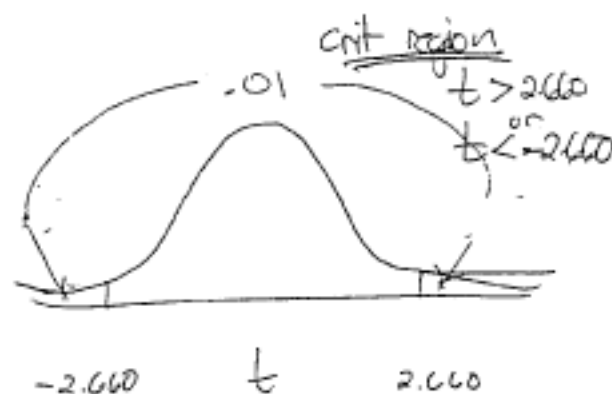
(change in scores from 10 years ago)

$\therefore s = \sqrt{\frac{SS}{n-1}}$   
 $= \sqrt{\frac{99}{99}}$

$= \sqrt{1} = 1$

$\alpha = .01$

Step 2 Estab. crit. region for t distrib.



Step 3 Sample data

$S_{\bar{x}} = \frac{s}{\sqrt{n}} = \frac{1}{\sqrt{100}} = \frac{1}{10}$

$t_{(99)}^{\text{obt.}} = \frac{\bar{x} - \mu}{S_{\bar{x}}}$   
 $= \frac{7.3 - 7.9}{.10}$   
 $= \frac{-0.6}{.10} = \underline{\underline{-6.00}}$

Step 4:) Reject  $H_0$  because  $t_{\text{obt.}}$  of  $-6.00$  is in crit region

Step 5:) Conclus: There is a significant change in scores from 10 yrs ago,  
 $t(99) = -6.00, p < .01.$

16)  $\mu = 21 \text{ g/day}$

sample  $n = 100$

$\bar{x} = 18.7$

$SS = 2475$

Step 1:

$H_0: \mu_{\text{amt eaten in humidity}} = 21 \text{ g.}$

(no effect of humidity on eating)

$H_1: \mu_{\text{amt eaten in humidity}} \neq 21 \text{ g.}$

(humidity affects amt rats eat)

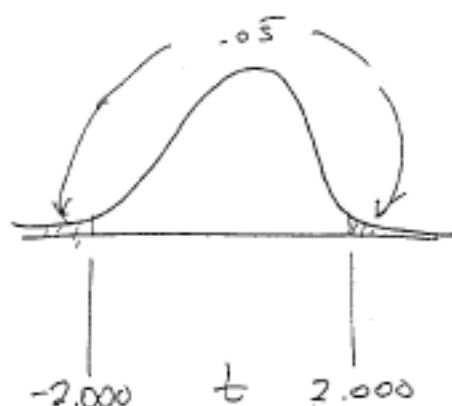
$\alpha = .05$

Step 2 Define critical region

$t > 2.000$

or

$t < -2.000$



$df = 100 - 1$   
 $= 99$

Step 3 sample data

$$t_{\text{obt}}(99) = \frac{\bar{x} - \mu}{S_x} = \frac{18.7 - 21}{.5} = -4.6$$

$$S_x = \frac{S}{\sqrt{n}}$$

$$S = \sqrt{\frac{SS}{n-1}}$$

$$= \sqrt{\frac{2475}{99}}$$

$$= \sqrt{25}$$

$$= 5$$

Step 4 Reject  $H_0$  because  $t_{\text{obt}}$  of  $-4.6$  is in the critical region

5) Conclude humidity significantly affected eating behavior,  $t(99) = -4.6$ ;  $p < .05$

$$\therefore S_x = \frac{S}{\sqrt{n}} = \frac{5}{\sqrt{100}} = .5$$

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Step 1

CSP Study

Scores: 18, 23, 24, 2

19, 28, 15, 26, 25

$$\bar{x} = \frac{\sum x}{n} = 22.25$$

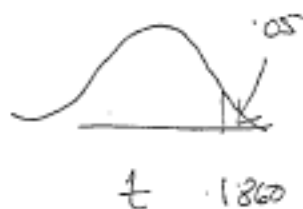
$$H_0: \mu_{\text{ESP folks score}} \leq 20 \quad (\text{no different than chance})$$

$$H_1: \mu_{\text{ESP folks score}} > 20 \quad (\text{better than chance})$$

$\alpha = .05$  one-tailed test

Step 2 Crit. region

$$t > +1.860$$



Step 3 sample data

$$t_{\text{obt}}(8) = \frac{\bar{x} - \mu}{s_{\bar{x}}} = \frac{22.22 - 20}{1.39} = 1.597$$

Step 4 Retain  $H_0$  because  $t_{\text{obt}}(8) = 1.597$  not in crit region

Step 5

Conclusion: ESP folks are not signif. better than chance,  $t(8) = 1.597$ ,  $p > .05$

$$s_{\bar{x}} = \frac{s}{\sqrt{n}}$$

$$s_{\bar{x}} = \frac{4.17}{\sqrt{19}} = 1.39$$

X	(x - $\bar{x}$ )	(x - $\bar{x}$ ) <sup>2</sup>
18	18 - 22.2 = -4.2	17.64
23	23 - 22.2 = .8	.64
24	24 - 22.2 = 1.8	3.24
22	22 - 22.2 = -.2	.04
19	19 - 22.2 = -3.2	10.24
28	28 - 22.2 = 5.8	33.64
15	15 - 22.2 = -7.2	51.84
26	26 - 22.2 = 3.8	14.44
25	25 - 22.2 = 2.8	7.84

$$\sum x = 200$$

$$\sum (x - \bar{x})^2 = 139.56$$

$$\sum x^2 = 4584$$

or

$$SS = \sum x^2 - \frac{(\sum x)^2}{n} = 4584 - \frac{(200)^2}{8} = 4444.44$$

$$= 139.55$$

$$s = \sqrt{\frac{\sum (x - \bar{x})^2}{n - 1}}$$

$$s = \sqrt{\frac{139.6}{8}}$$